

1 **Polymer lattice-reinforcement for enhancing ductility of concrete**

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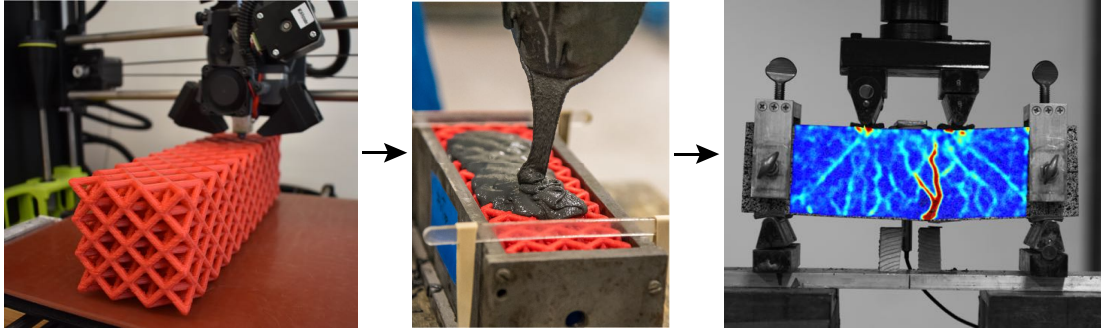
9 **Highlights**

- 10 • Ultra-high-performance concrete was reinforced with 3D-printed, stretch-dominated
11 polymeric lattices, resulting in greatly increased ductility
- 12 • Ductility was optimized by deliberately orienting 3D printed polymer filaments in line with
13 the expected tensile stresses.
- 14 • The ductility-enhancing mechanisms during flexure are associated with multiple cracking
15 and tortuous crack paths.
- 16 • This fabrication method allows easy pouring of the mortar mixture, unlike polymer fiber-
17 reinforced composites.

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- 18 • This composite production method lends itself more readily to automated manufacturing than
19 conventional steel rebar-reinforced concrete.

20 Graphical abstract



22 Abstract

23 Concrete is the most widely used engineering material. While strong in compression, concrete is
24 weak in tension and exhibits low ductility due to its low crack growth resistance. With increasing
25 compressive strength, concrete becomes even more brittle, hence requiring appropriate
26 reinforcement to enhance its ductility. This paper presents a new method for increasing the
27 ductility of ultra-high-performance concrete by reinforcing it with 3D printed polymeric lattices
28 made of either polylactic acid (PLA) or acrylonitrile butadiene styrene (ABS). These lattice-
29 reinforced concrete specimens were then tested in compression and four-point bending. The
30 effect of polymeric reinforcement ratios on mechanical properties was investigated by testing
31 two lattice configurations. The lattices were very successful in transforming the brittle ultra-
32 high-performance concrete (UHPC) into a ductile material with strain hardening behavior; all
33 flexural specimens revealed multiple cracking and strain hardening behavior up to peak load.
34 Increasing the ABS reinforcing ratio from 19.2% to 33.7% resulted in a 22% reduction in
35 average compressive strength. However, in flexure, increasing the PLA reinforcing ratio from
36 19.2% to 33.7% resulted in a 38% increase in average peak load. The compression results of all

37 specimens independent of their reinforcement ratio revealed smooth softening behavior in
38 compression.

39 **1. Introduction**

40 Concrete strikes a balance between performance, cost, and availability. It has enabled many of
41 the largest and most demanding engineering projects in the world, and also finds its place in less
42 grandiose projects such as home foundations and sidewalks. On its own, the brittle tensile
43 response and quasi-brittle compressive response of concrete would limit its usefulness to simple,
44 compression-only load cases. As such, it relies on the composite behavior provided by the
45 reinforcement to provide ductile, predictable response under many types of loading demands.

46 Steel rebar cages are traditionally used to provide the requisite reinforcement and can be
47 detailed to effectively resist certain load cases — but they also come with limitations. As
48 structural elements trend toward more slender beams and columns using higher strength
49 concrete, conventional reinforcement detailing may not be enough to resist large demands such
50 as seismic or blast loading. Furthermore, rebar cages with high reinforcing bar ratios are not only
51 very labor-intensive to construct but also difficult to infiltrate with concrete.

52 An alternative way to enhance the ductility of concrete is through the use of discrete steel
53 or polymer fibers. However, the fiber distribution in fiber-reinforced concrete composites cannot
54 be easily controlled, hence leaving sections for the cracks to propagate uninhibited [1–6]. This
55 heterogeneity leads to unpredictability in the overall performance of fiber reinforced composites
56 and can reduce the expected tensile strength and fracture toughness of the material [7]. The
57 continuity and predictability inherent to three-dimensional reinforcements could potentially be
58 the key to mitigating these issues.

59 Textile reinforced concrete (TRC) uses a similar principle, but in two dimensions, and
60 has been shown to provide excellent reinforcement. Being reinforced in only two dimensions,
61 however, TRCs have limited usefulness in structural applications, and are mainly used in repair
62 and in lightweight sandwich panels [8–15].

63 This paper investigates a new class of composites that utilizes three-dimensional lattice
64 structures as reinforcements to enhance the ductility of concrete. Here, we employ the octet-truss
65 geometry because it is known for its high specific stiffness and fracture toughness [16,17]. The
66 octet lattices were prototyped in acrylonitrile butadiene styrene (ABS) and/or polylactic acid
67 (PLA) using Fused Deposition Modeling (FDM) 3D printers. The use of a polymeric
68 reinforcement material — instead of a steel reinforcement — enables the polymer-reinforced
69 structures to be more lightweight, corrosion-resistant, and thermally insulating.

70 Previous research has used 3D printed polymers to reinforce cementitious material. The
71 present authors [18] provided the first investigation of three-dimensional octet lattice-reinforced
72 cementitious materials and found increased ductility while using a highly workable mortar.
73 Farina et al. reinforced cement mortar with polymeric ‘fibers’ — in the form of simple, discrete
74 7.5 mm-diameter cylindrical bars — that were 3D printed from a photopolymer resin [19]. They
75 found that augmenting the surfaces of the printed reinforcement cylinders with mm-scale
76 protrusions led to much greater strain hardening of the composite than did smooth reinforcement
77 rods of the same diameter and material. Samples with roughened reinforcement showed shear
78 failure under three-point bend tests, whereas structures reinforced with smoother cylinders
79 exhibited flexural failure. Nam et al., meanwhile, investigated the effects of reinforcement
80 orientation and distribution by 3D printing reinforcement networks of connected photopolymer
81 resin fibers with varying spatial distributions. They found some evidence of higher peak bending

82 strength when using a triangulated reinforcement structure whose mesh was denser in regions of
83 higher tensile stress [20]. However, the inherent brittleness of the cement was not significantly
84 mitigated in any of the specimens, possibly because of the relatively low volume fraction of
85 polymer reinforcement used.

86 Recently, Rosewitz et al. developed bio-inspired cement–polymer composites, and
87 evaluated a variety of cellular polymeric reinforcement structures which showed increased
88 ductility and, in some cases, higher peak strength than unreinforced mortar [21]. Xu et al. [22]
89 tested the performance of thin panels reinforced with honeycomb lattices manufactured in ABS
90 using FDM. Their panels demonstrated ductility and multiple cracking when tested in flexure.
91 Both Rosewitz’s and Xu’s work, however, used prismatic or “two-dimensional” reinforcement
92 geometries, which may limit their applicability to complex geometries or loading states.

93 Previous work, then, has shown the great potential of polymeric reinforcement, but
94 highlighted several areas where further work was needed before widespread adoption. Firstly, a
95 systematic means of incorporating fully 3D — as opposed to prismatic or 2D — reinforcement is
96 needed, to accommodate potentially complex cast geometries and loading requirements.
97 Secondly, the specific polymeric materials and printing method need to offer a plausible route
98 towards scaling up the process. To this end, extrusion of thermoplastic polymers offers a more
99 realistic prospect of large-scale production than the use of photopolymers, which tend to be
100 much more expensive than commodity thermoplastics per unit mass. Moreover, thermoplastic
101 extrusion can be scaled up by increasing nozzle diameter and using robotic printers, whereas
102 photopolymer deposition rates and printing volumes remain more limited, in spite of recent
103 progress.

104 The study presented here expands significantly upon our original demonstration of
105 polymeric lattice reinforcement [18] by providing more comprehensive data on the effect of
106 three-dimensional octet lattices on the mechanical performance of concrete. Crucially, whereas
107 the previous study used a conventional mortar, this study concentrates on reinforcement of an
108 ultra-high-performance-concrete (UHPC) which has previously been developed by some of the
109 present authors [23–26]. Polymer lattice reinforcement of UHPC would be particularly
110 advantageous: because of the advanced mortar’s higher cost of production, optimized
111 reinforcement geometries that can limit the amount of mortar used in a particular application
112 would significantly expand its potential uses. Moreover, one of the objectives of UHPC in the
113 first place is to reduce the amount of cement and associated CO₂ emissions required for a given
114 load, and using a reinforcement strategy in which a significant volume fraction is *non-*
115 cementitious can compound this advantage. Such a strategy is shown in this work, with
116 polymeric volume fractions exceeding 30% in some cases. The polymeric phase could in
117 principle be made from recycled material, cutting the carbon footprint further.

118 UHPC is, however, far more brittle than normal concrete, and hence may be expected to
119 interact mechanically with the reinforcement in different ways and to be more difficult to
120 enhance in ductility. It is therefore important to study whether the same degree of ductility
121 enhancement can be achieved in UHPC as in conventional mortar, and with what degree, if any,
122 of peak strength loss.

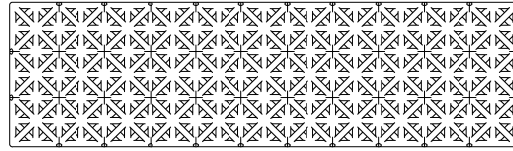
123 In this paper, we show how UHPC’s ductility can be successfully increased with 3D
124 reinforcement lattices printed from PLA or ABS, which are widely used in additive
125 manufacturing and are available at reasonable cost. ABS is certainly already used for concrete
126 reinforcement — for example, the carbon fiber-reinforced ABS in the “C-Fab” process marketed

127 by Branch Technology [27]. For very high production volumes and rates, lattices could
128 potentially be manufactured using other processes, including modified molding or casting
129 processes. Additionally, while in this work we explore geometrically regular 3D lattices, there is
130 the potential to spatially vary the lattice parameters — such as the polymer volume fraction — to
131 accommodate complex loading conditions. It may even be possible to localize reinforcement
132 material in regions where tensile loads are predicted, thereby optimizing the use of polymeric
133 material.

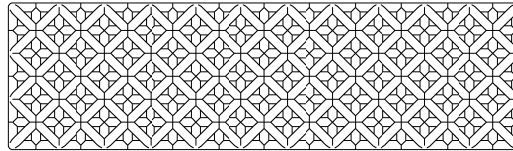
134 **2. Materials and methods**

135 2.1 Octet lattice design

136 Two configurations of octet lattices were fabricated as reinforcements for the ultra-high-
137 performance concrete: one with a low volume reinforcement ratio (19.2%) and one with a high
138 volume reinforcement ratio (33.7%). The higher reinforcement of 33.7% was achieved by
139 increasing the member diameter of the octet unit cells, as shown in Figure 1. The member
140 diameters were chosen to ensure that they were several times greater than the extrusion nozzle
141 diameter of the 3D printer used (nozzle diameters were 1.2 mm for the flexural specimens and
142 0.4 mm for the compressive specimens), meaning that the octet geometry could be resolved
143 accurately and repeatably by the printer. The unit cell lengths of 11.7 and 23.5 mm were selected
144 to be large enough that the cement mix could flow easily through the interstices of the lattice,
145 and yet small enough that multiple unit cells could be incorporated into a sample that could be
146 printed in a reasonable time and whose size was manageable for testing. The member diameter
147 and unit cell lengths in turn determined the lattice volume fractions.



(a)



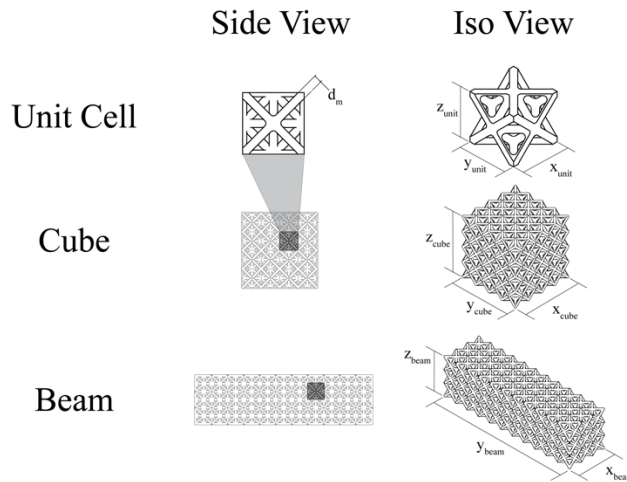
(b)

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Figure 1 – the two octet lattice designs. (a) 19.2% volume fraction and (b) 33.7% volume fraction. The lattice in (b) has thicker members, and thus a higher volume fraction than (a).

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Cube and beam shaped lattices as shown in Figure 2 were 3D printed. These lattices were then infiltrated with an ultra-high-performance concrete and tested in compression and four-point bending, respectively. The specimens’ dimensions were chosen so that there were at least three unit cells in any direction, and are given in Table 1.



155
156

Figure 2 - Cube and beam lattice specimen descriptions

157

Table 1 - Geometry description for compression cube and flexural beam specimens

Specimen description	Member diameter, d_m (mm)	Lattice bounding dimensions (mm^3)	Lattice-reinforced concrete bounding dimensions (mm^3)	Number of lattice unit cells across	Unit cell length, x_{unit} (mm)
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Compression cubes	19.2% design	1.6	$48.5 \times 48.5 \times 48.5$	$50.8 \times 50.8 \times 50.8$	$4 \times 4 \times 4$	11.7
	33.7% design	2.3	$49.3 \times 49.3 \times 49.3$			
Flexural beams	19.2% design	3.2	$73.6 \times 73.6 \times 261.3$	$76.2 \times 76.2 \times 279.4$	$3 \times 3 \times 11$	23.5
	33.7% design	4.6	$74.9 \times 74.9 \times 262.8$			

158 While the octet's volume percentages remained the same for compressive and flexural
159 specimens, the scale of the octet structure changed. The octets are doubled in scale for flexural
160 specimens compared to the compressive specimens; the octet member diameters and unit cell
161 lengths are listed in Table 1.

162 2.2 Fabrication

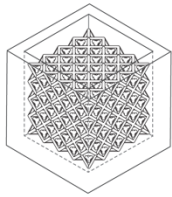
163 The lattice prisms for the flexure tests were 3D printed with PLA on a LulzBot TAZ 6 machine
164 using a 1.2 mm diameter nozzle, as shown in Figure 3a. The 1.2 mm diameter nozzle is rather
165 coarse, which allows each beam to be printed in less than 24 hours. The thermomechanical
166 properties of PLA allowed these lattices to be printed without any support structures. To
167 fabricate the compression cubes from PLA, a BCN3D Sigma with a 0.4 mm nozzle diameter was
168 used which also did not require any support material. The ABS cube lattices were produced
169 using a Stratasys Dimension 1200es with T16 model tip using Stratasys ABSPlus model material
170 and Stratasys P400SR support material. After printing, the support material was dissolved in an
171 ultrasonic bath of 2% concentration sodium hydroxide (Stratasys WaterWorks).

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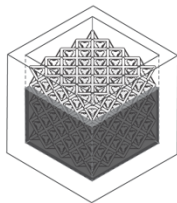
(a)



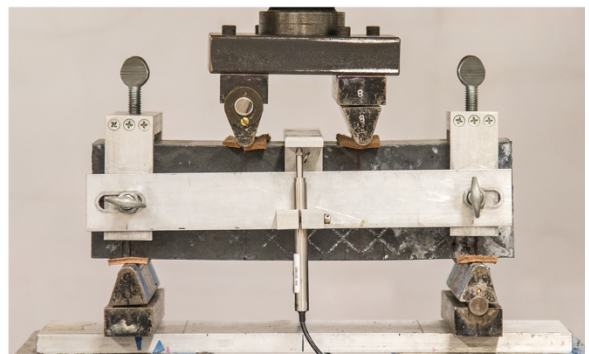
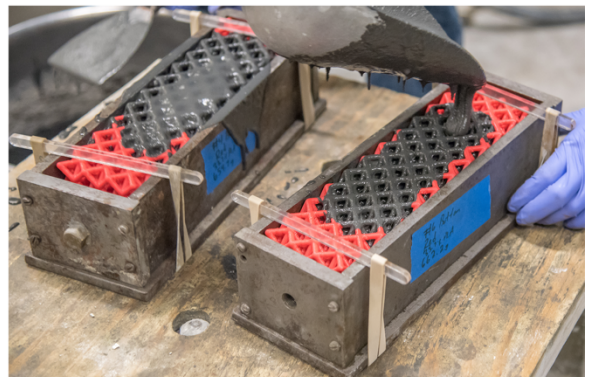
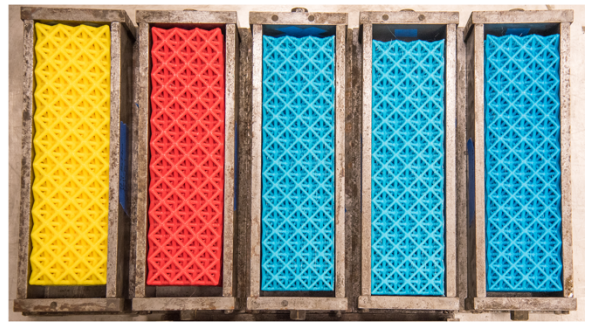
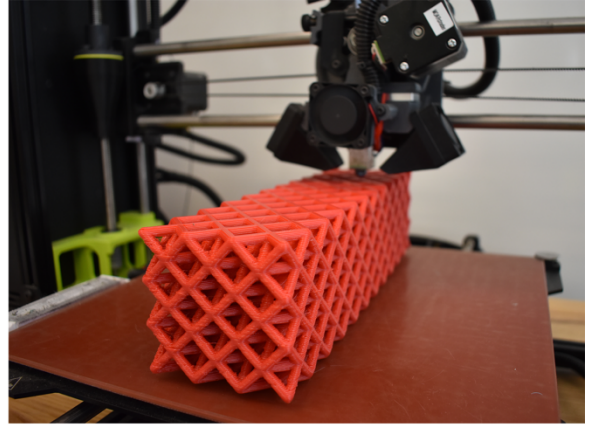
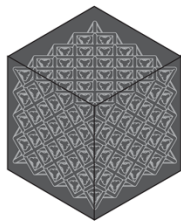
(b)



(c)



(d)



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Figure 3 - Fabrication of lattice-reinforced concrete beams. (a) 3D printing of the polymeric lattice, (b) placement of lattices of different reinforcing ratios inside molds, (c) infiltration of the lattices by an ultra-high-performance concrete, and (d) cured beam ready to be tested.

177 Both cube and prism lattices were infiltrated with an ultra-high-performance concrete; the
178 UHPC's weight proportions are listed in Table 2. The 7-day compressive strength of a similar
179 UHPC is 119 MPa; further information on the UHPC mixture, development, and mechanical
180 properties may be found in [23–26]. To create lattice-reinforced concrete beams, the lattices
181 were placed into molds (Figure 3b), and the lattices' orientations were controlled so that the
182 flexural tests' loading direction was aligned with the printer's build direction. Having the tension
183 in the specimens aligned with the printed filaments ensures optimal mechanical properties. The
184 lattices were then infiltrated with UHPC (Figure 3c), and a vibration table was used to assist with
185 the infiltration. The addition of fly ash and superplasticizer resulted in a highly workable
186 concrete, which allowed each lattice to be fully infiltrated. The same procedure was followed to
187 cast lattice-reinforced concrete cubes.

188 The performance of the lattice-reinforced specimens is compared to a plain UHPC beam
189 and an ultra-high-performance fiber-reinforced concrete (UHPFRC) beam reinforced with 1.4%
190 PLA fibers (6 mm length, 1.3 denier per filament). Note that 1.4% by volume of fibers was the
191 highest volume percent that could be incorporated into the UHPC mix while still allowing the
192 mix to be workable enough to cast a rectangular beam.

193 All beams and cube specimens were stored and cured in a fog room (with 95% relative
194 humidity at room temperature) before testing on day 7.

195

196

197

198 *Table 2 - Weight proportions for the ultra-high-performance concrete mix*

Ingredient	Weight proportion
Cement	1.0
Fly ash	0.1
Water	0.26
Superplasticizer	0.02
Silica sand 1 (460 μm)	0.6
Silica sand 2 (120 μm)	0.3
Glass powder	0.25
Silica fume	0.25

199

200 2.3 Uniaxial compression and four-point flexural tests

201 Mechanical testing was carried out on a Universal Testing Machine with a 530 kN load cell. The
 202 eight compression tests were performed according to ASTM C109 [28]. The nine beam
 203 specimens were tested in four-point bending according to ASTM C1609 [29] with a 22.9 cm
 204 span length. For both compression and flexural tests, the displacements were measured with two
 205 linear variable differential transformers (LVDTs) — one at the front of the specimens, and one at
 206 the back — and the measurements were averaged to compute the midspan deflection. On one of
 207 the 19.2% lattice-reinforced beams, and one of the 33.7% lattice-reinforced beams, a digital
 208 image correlation (DIC) technique was utilized instead of a second LVDT. For these two beams,
 209 spackle patterns (black dots on a white background) were spray-painted onto the front side and a
 210 Canon EOS 6D camera with a 100 mm macro lens then captured the displacement on the front
 211 side. The midspan deflection was then determined by averaging the displacement measured with
 212 DIC and the displacement measured with the LVDT.

213 **3. Results and discussion**

214 3.1 Uniaxial compression results

215 The lattice-reinforced UHPC's uniaxial compression results and the number of specimens tested
216 are given in Table 3. Both the PLA and ABS lattice-reinforced cubes exhibit a lower
217 compressive strength at the higher reinforcement percentage of 33.7% than at 19.2% polymer
218 volume fraction. While only one PLA specimen was tested for each reinforcing ratio, the results
219 suggest a common trend with the ABS results, whereby an increase in reinforcing ratio from
220 19.2% to 33.7% leads to a reduction in compressive strength. The smaller volume of UHPC at
221 33.7% lattice-reinforcement is responsible for the strength reduction since less of the high
222 compressive-modulus UHPC is being incorporated into these lattices. A large reduction in
223 strength was observed with the 33.7% ABS lattice-reinforced cubes. Both the 19.2% and 33.7%
224 ABS lattice-reinforced cubes show high strains at the peak stress, as well as high strain energy
225 densities. The 95% confidence intervals for the mean strain energy densities overlap for the
226 19.2% and 33.7% ABS-reinforced specimens.

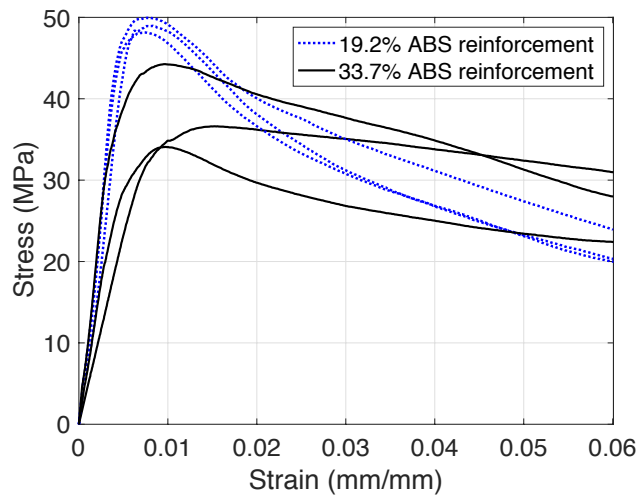
227 *Table 3 - Description and results of uniaxial compression tests. Values indicate 95% confidence intervals of the mean.*

Cube description	Compressive strength (MPa)	Strain at peak stress (mm/mm)	Strain energy density (MPa)
19.2% PLA lattice-reinforcement (N = 1)	45.3	0.0114	1.86
33.7% PLA lattice-reinforcement (N = 1)	43.4	0.0161	2.09
19.2% ABS lattice-reinforcement (N = 3)	49.0 ± 1.0	0.0079 ± 0.0005	1.94 ± 0.13
33.7% ABS lattice-reinforcement (N = 3)	38.3 ± 6.0	0.0116 ± 0.0036	1.88 ± 0.32

228 N = number of specimens

229 Figure 4 shows the compressive stress–strain curves for the two types of reinforcement
230 ratios: three curves for the 19.2% ABS lattice-reinforced UHPC cubes, and three curves for the
231 33.7% ABS lattice-reinforced UHPC cubes.

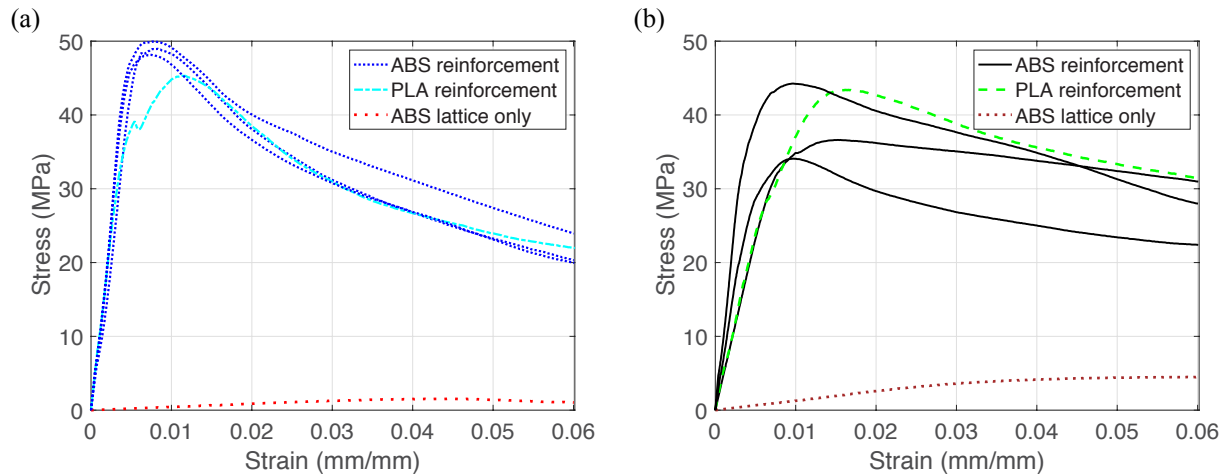
232 The concrete cubes with the larger amount of reinforcement exhibit a larger variability in
233 stress–strain behavior, as shown by both Figure 4 and by the 95% confidence intervals for the
234 compressive strength shown in Table 3. The larger variability in the 33.7% lattices may be
235 caused by their smaller openings compared to the 19.2% lattices, which makes their infiltration
236 with UHPC more difficult and hence less uniform (due to possible air voids). On the other hand,
237 these composites exhibit smooth softening behavior up to high strain levels. In comparison,
238 UHPC (not shown here) does not exhibit softening behavior due to its high brittleness.



239
240 *Figure 4 - Compressive stress-strain curves for ABS lattice-reinforced UHPC with 19.2% reinforcement and 33.7%*
241 *reinforcement.*

242 The compressive stress-strain curves for both ABS and PLA lattice-reinforced UHPC at
243 19.2% and 33.7% reinforcement, respectively, are shown in Figure 5. At both reinforcement
244 ratios, the ABS and PLA lattice-reinforced samples perform similarly, as they exhibit similar
245 compressive strengths and strain energy densities. From these results, it appears that PLA-
246 reinforced UHPC may reach a higher strain at peak energy than ABS reinforced UHPC, but the

247 overall stress–strain curve characteristics are highly similar, and more tests need to be conducted
248 to form statistical conclusions. Figure 5 also shows the compressive behavior of the ABS lattices
249 (without UHPC), and while both the 19.2% and 33.7% ABS lattices exhibit high ductility, they
250 also exhibit low compressive strengths.



252 *Figure 5 - Compressive stress-strain curves. The response of the pure lattice and the UHPC reinforced with PLA and ABS*
253 *lattices is shown in (a) for 19.2% reinforcement and in (b) for 33.7% reinforcement.*

254 3.2 Four-point bending results

255 The flexural results of the PLA lattice-reinforced UHPC specimens are summarized in Table 4.
256 Note that all flexural specimens use PLA and not ABS, since PLA lattices do not require support
257 structures to print at this scale, but ABS lattices would require the extra steps to dissolve the
258 support material.

259 In these four-point bending tests, the 33.7% lattice-reinforced beams exhibit a higher
260 peak load than the 19.2% lattice-reinforced beams. Both the 19.2% and 33.7% lattice-reinforced
261 beams show high deflections at peak load and high toughness. The 95% confidence intervals for
262 the mean toughness overlap for the 19.2% and 33.7% reinforcement ratios.

263 Table 4 – Four-point flexure results. Values indicate 95% confidence intervals of the mean.

Beam description	Peak load (kN)	Deflection at peak (mm)	Toughness (kN·mm)*
19.2% PLA lattice-reinforcement (N = 3)	14.6 ± 0.4	1.8 ± 0.4	17.5 ± 0.5
33.7% PLA lattice-reinforcement (N = 4)	20.1 ± 4.3	2.4 ± 0.6	17.5 ± 0.9
UHPC only (N = 1)	13.0	0.027	0.20
1.4% PLA fiber-reinforcement (N = 1)	6.6	0.021	0.10

264 N = Number of specimens

265 * Toughness at 1.52 mm midpoint deflection

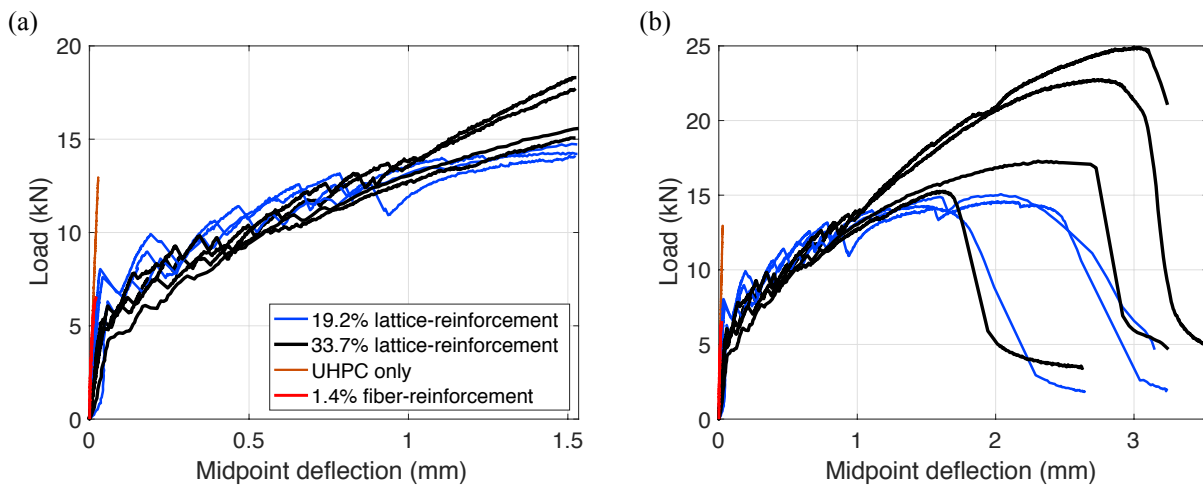
266 The load–midpoint deflection curves of the flexural beams are shown in Figure 6. For midpoint
 267 deflections up to 1.52 mm (*i.e.* the span length divided by 150, as specified by [28]), all
 268 specimens behave similarly, independent of their reinforcing ratios (Figure 6a). The behavior
 269 differs at larger deflections, where the beams with a higher reinforcement ratio achieve higher
 270 loads (as shown in Figure 6b), which is opposite to the compression results. This difference in
 271 behavior at higher deflections is due to the increased crack growth resistance that a larger
 272 reinforcement ratio provides.

273 Similar to the compression results the beams with the higher reinforcement ratio exhibit a
 274 larger variability in their load–deflection curves due to the small openings of the 33.7% lattices
 275 that make the infiltration of UHPC less uniform. Figure 6b shows one 33.7% lattice-reinforced
 276 beam which underperforms compared to the other three samples; however, since its net
 277 deflection at peak load is not more than 1.5 interquartile ranges below the first quartile and it is
 278 not more than 1.5 interquartile ranges above the third quartile, we do not classify it as an outlier.

279 While all lattice-reinforced beams reveal high ductility, the beam reinforced with
 280 1.4 vol% PLA fibers shown in Figure 6 by the red line exhibits very brittle behavior up to failure.

281 Hence, the highest volume fraction of fibers that could be incorporated into the UHPC mixture
282 while maintaining a workable mix was not sufficient to provide any crack growth resistance.
283 While the volume fractions of polymer fibers and printed reinforcement used in this work are
284 very different (1.4 vol% fibers vs 19.2–33.7 vol% lattices), the results shown for PVA fiber
285 reinforcement represent the best practically achievable option with this particular reinforcement
286 approach and mortar composition.

287 The brittle performance of the plain UHPC beam agrees with the mechanical properties
288 of a similar UHPC tested in [26]. In comparison to the unreinforced, UHPC-only beam, the
289 lattice-reinforced beams are able to achieve higher flexural loads, since the reinforcement
290 prevents a dominant crack from propagating through the beam.

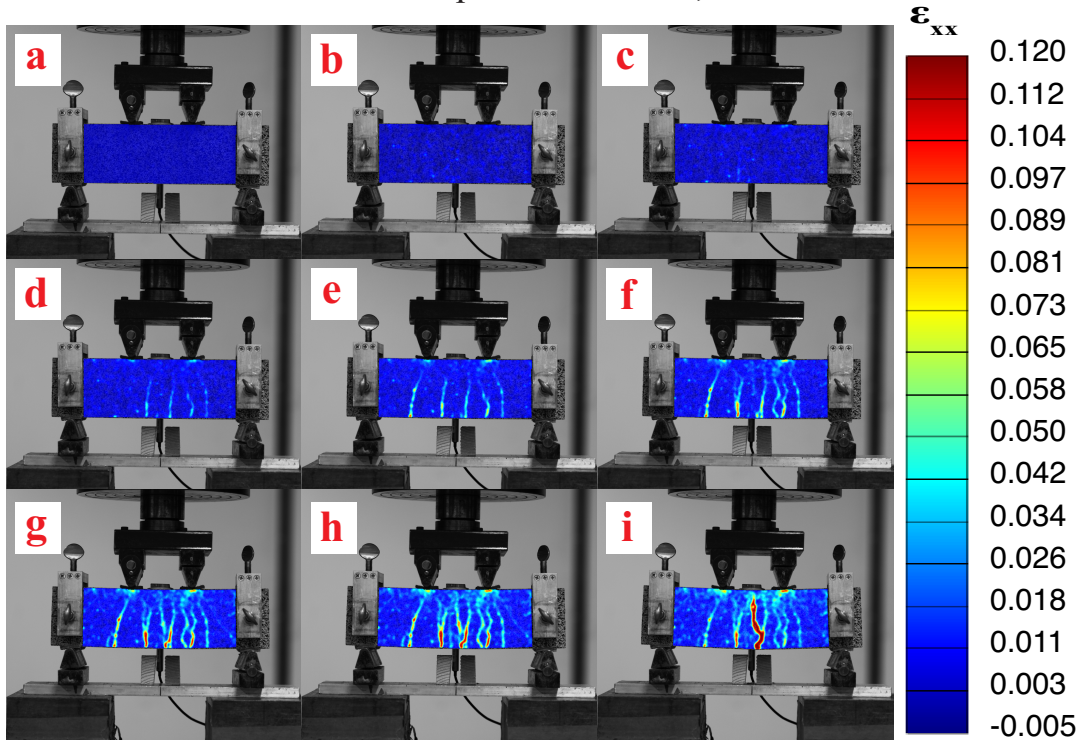
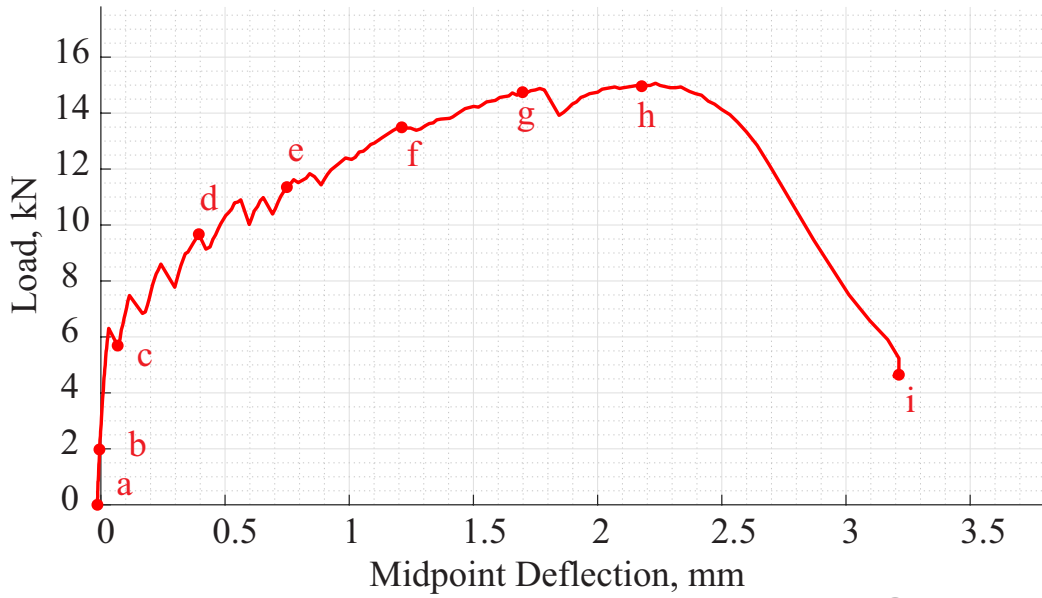


291
292 *Figure 6 – Load–deflection curves for flexural specimens with varying amounts of polymeric reinforcement. The loading curve is*
293 *plotted (a) until a maximum deflection of 1.52 mm (which was used for the toughness calculations in Table 4) and (b) until*
294 *failure of the beams.*

295 296 3.3 Failure characteristics

297 DIC software (OpteCAL) was utilized to investigate the sequence of crack initiation and crack
298 pattern of a 19.2% lattice-reinforced beam during four-point bending. Figure 7 shows the strain

299 field across the front face of the specimen. The strain field is then correlated with the load-
300 deflection curve.



301
302 *Figure 7 - Strain field across the front surface of flexural beams as measured with digital image correlation techniques. The*
303 *progression of cracks is shown at various points across the load-deflection curve for the 19.2% lattice-reinforcement beam.*

304 From (a) to (b), while the beam is in its elastic regime, no cracking could be observed.
305 Hairline cracks initiate between (b) and (c), followed by multiple crack formation at (d). The
306 multiple cracks increase in width from (d) to (f) in the tension zone while propagating towards
307 the compression zone. Each of the multiple cracks continue to carry load, bifurcate and further
308 increase in width between (g) and (h), which causes a flattening of the load–deflection curve.
309 Eventually one of the multiple cracks becomes the dominant crack which leads to a drastic
310 reduction in load capacity of the beam. The strain field of the specimen just prior to failure is
311 shown in (i), with the dominant crack visible in red. DIC analysis for a 33.7% lattice-reinforced
312 beam (not shown here) shows failure mechanism trends that are identical to the mechanisms
313 exhibited by this 19.2% lattice-reinforced beam, with the 33.7% lattice-reinforced beam
314 exhibiting a higher ultimate load.

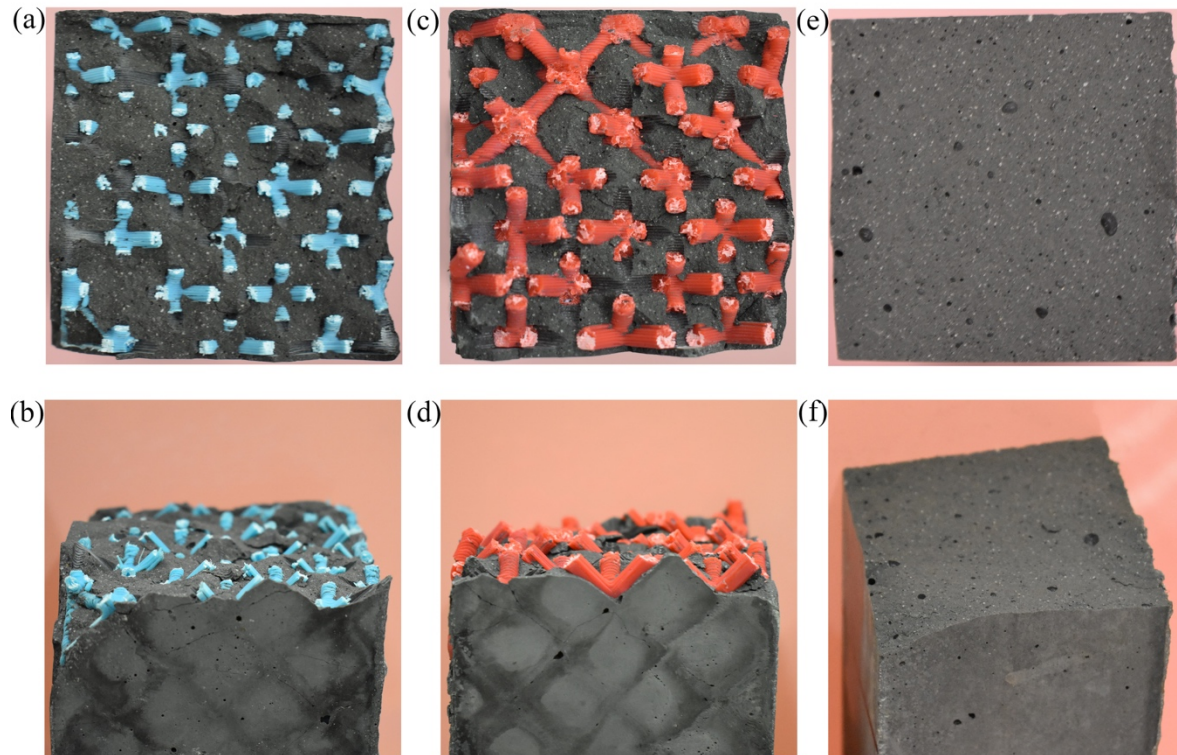
315 Figure 8 contains images of representative fracture surfaces and side views of a 19.7%
316 lattice-reinforced beam (Figure 8a, b), a 33.7% lattice-reinforced beam (Figure 8c, d), and the
317 1.4% fiber-reinforced beam (Figure 8e, f). Both lattice-reinforced beams reveal rough fracture
318 surfaces which indicates that the cracks traveled through a tortuous path. This type of cracking
319 contributes to the high ductility observed in these lattice-reinforced beams. The images of the
320 lattice-reinforced beams also show step marks in the concrete, which are locations where the
321 concrete debonded from the polymeric lattice, leading to high strain energy density values. The
322 polymeric members show stress-whitening, indicating that they carried tensile stresses.
323 Furthermore, the polymeric members' cup-and-cone fracture surfaces suggest that the fracture
324 was ductile.

325 By contrast, the fiber-reinforced beams show smooth fracture surfaces, with no detectable
326 fiber pull-out. This type of fracture surface is indicative of either a lack of debonding between

327 the fibers and the matrix or inhomogeneous fiber distribution due to the low workability of the
328 mix. Lattice-reinforcement has the advantage that it allows us to control precisely the distribution
329 of the reinforcement within a structure.

330 Whereas in Salazar et al. [18], the polymeric lattice of the lattice-reinforced mortar
331 samples fractured uniformly along a plane, the lattice-reinforced UHPC shown here does not
332 have the polymeric members fracture along a single plane. The difference is due to the print
333 direction, as previous research has shown that aligning the printed layers to be perpendicular to
334 the crack plane results in increased tensile strength and fracture toughness [30,31]. The current
335 work has the lattices printed in such a way that the build direction is aligned with the loading
336 direction, as opposed to having the build and loading directions be orthogonal as in [18], which
337 allowed the crack to cleave in-between printed layers.

338



339

340 *Figure 8 - Direct and side views of fracture surfaces of flexure specimens. (a) and (b) are representative of the 19.7% lattice-*
 341 *reinforced beams; (c) and (d) represent the 33.7% lattice-reinforced beams; (e) and (f) are the fiber-reinforced beam. Note that*
 342 *the dominant crack did not propagate through the entire beam, and beams were opened manually post-testing.*

343 4. Conclusion

344 Lattice-reinforced concrete samples were created by fabricating polymeric lattices and
 345 infiltrating these lattices with ultra-high-performance concrete. These lattice-reinforced concrete
 346 samples exhibited high ductility in both compression and flexure. Compressive tests showed
 347 high strain density values, with the polymeric material choice (PLA or ABS) not having a
 348 significant effect. Increasing the percentage of the lattice reinforcement, however, led to a
 349 decrease and a higher variability in their compressive strength. Regarding flexure, all lattice-
 350 reinforced beams exhibited strain hardening up to peak load and the highest peak loads were
 351 observed with the higher lattice reinforcement of 33.7%. DIC was utilized to investigate the
 352 strain fields and to obtain information on the crack pattern during flexural loading. The results

353 revealed multiple cracking and crack widening in these octet lattice-reinforced beams up to peak
354 load.

355 While this paper focused on 3D-printed PLA and ABS octet lattice-reinforced structures
356 as proofs of concept, the method itself is not limited to this specific kind of lattice geometry or to
357 these particular polymeric materials. The ideal reinforcement geometry and material will depend
358 on the application. Lattice reinforcement allows the placement of the reinforcement material to
359 be controlled and hence optimized for specific loading scenarios — for example by increasing
360 the volume fraction of reinforcement material in regions of higher expected tensile stress.
361 Moreover, the optimal choice of polymeric material is a matter for future study, and the long-
362 term stability of candidate polymers in contact with cementitious materials will need to be tested.

363 Fused deposition modeling 3D printing is known to be an anisotropic process, with 3D-
364 printed components being stronger when loaded along extruded polymer filaments, and weaker
365 when loaded across the interfaces between adjacent filaments. In this paper the specimens were
366 printed such that the build direction was aligned with the flexural tests' loading direction.
367 Therefore, the tension in the samples was predominantly aligned with the printed filaments. In
368 this case, the cracks are forced to propagate through multiple printed layers, and not solely
369 between layers. This approach allowed our specimens to reach as high a toughness as possible
370 for the chosen manufacturing process.

371 The choice of 3D printing for lattice fabrication enabled rapid prototyping. Fabrication at
372 larger scales and volumes — such as for building construction — could be accomplished by
373 robotic extrusion printing with larger nozzles; the higher material deposition rates would
374 substantially reduce production times. Indeed, the use of large-scale robotic extrusion printers in

375 which individual extruded filaments of polymer are typically 5–10 mm in diameter would not
376 only increase throughput but would also eliminate layering effects within the members of the
377 printed lattices, since a single large extruded filament could serve as a complete member. If the
378 member and unit cell sizes of these lattices were to be increased to aid high-volume production,
379 while the materials remained similar, it can be anticipated that the basic failure mechanism
380 would remain the same, although this would need to be confirmed through further experiments.

381 It may also be possible to develop injection-molding processes for geometrically regular
382 reinforcement lattices. The octet lattice geometry is defined by approximately triangular,
383 intersecting prismatic voids, so in principle a mold could be engineered with multiple retractable,
384 interlocking cores to create the 3D lattice. While the development costs of such an approach
385 would probably be very considerable, they may be warranted by the increased production rate.
386 Layering and directional effects could also be minimized by molding rather than printing.

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396 **Data Availability**

397 The raw data required to reproduce these findings are available to download from
398 <http://dx.doi.org/10.17632/wv7hvgg8c7.1>

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