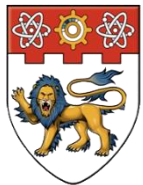


# Performance-based Engineering Approach to the “**Best**” Decision for Energy-efficient and Sustainable Building Design

H. Lee, K.M. Mosalam & S.P. Chiew

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# PBE-Approach to the Holistic Best Design Decision

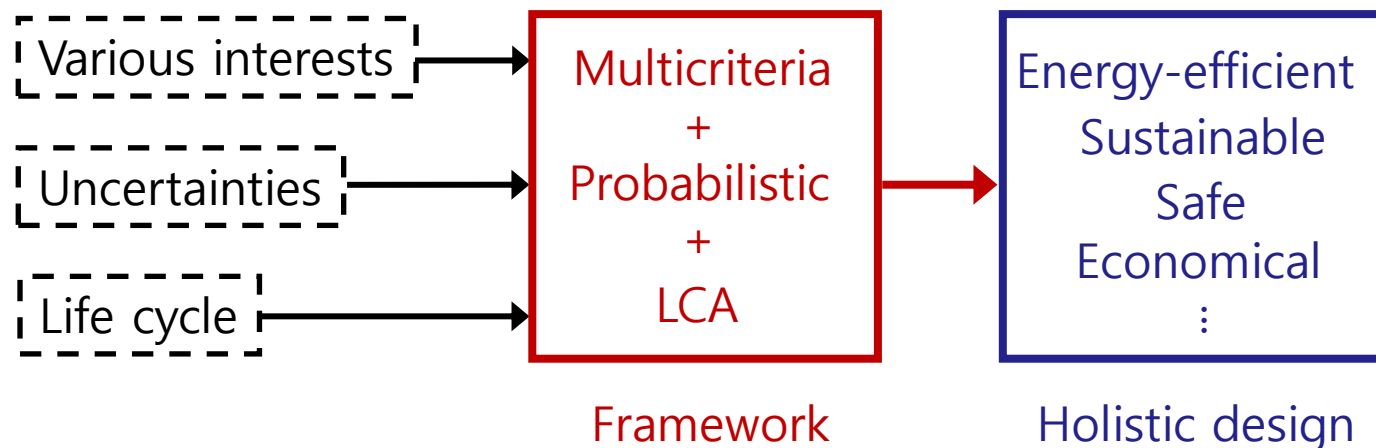
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## □ Objective

Develop a framework to make the best decision for building design, which is

- ✓ Energy-efficient
- ✓ Sustainable
- ✓ Safe
- ✓ Economic, etc.

considering interests of various stakeholders and accounting for all sources of uncertainties during the life cycle of the building.



# PBE-Approach to the Holistic Best Design Decision

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## □ Decision-Making Process:

### MIVES (Model for Integration of Values for Evaluation of Sustainability)

#### 4 steps:

- Tree Construction
- Value Function
- Weight Assignment
- Selection Amongst Alternatives

# PBE-Approach to the Holistic Best Design Decision

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## □ MIVES: Decision-Making Process

### ▪ Tree Construction

San José and Garrucho (2010); Pons (2011)

The branches of a tree should accomplish the followings:

- ✓ Relevance
- ✓ Difference-making for each one of the alternatives
- ✓ Minimal number of items

Iyengar (2012) [<http://www.trendhunter.com/keynote/sheena-iyengar>]

- ✓ **Cut**: Use 3 levels of unfolded branches, and every branch to have 5 sub-branches or less in the successive unfolding steps;
- ✓ **Concretize**: Use indicators that experts and stakeholders can understand;
- ✓ **Categorize**: Use more categories and fewer choices; and
- ✓ **Condition**: Gradually increase the complexity.

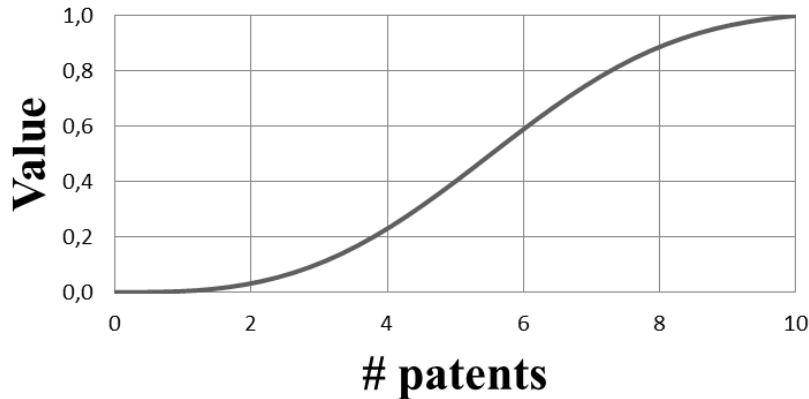
# PBE-Approach to the Holistic Best Design Decision

## □ MIVES: Decision-Making Process

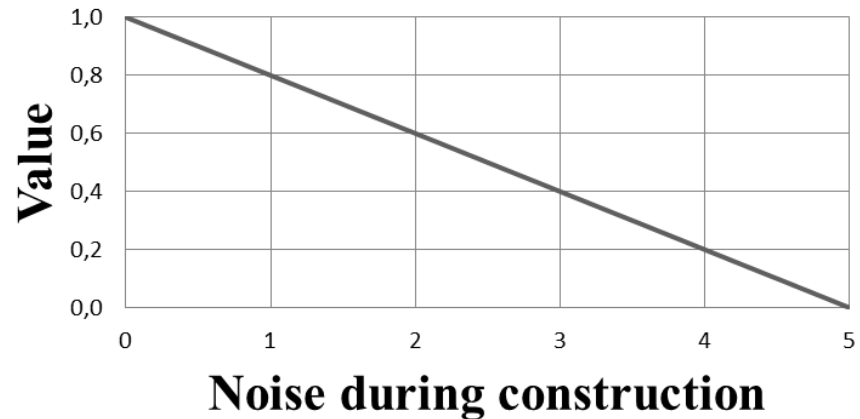
### ▪ Value Functions

- ✓ Non-negative increasing/decreasing functions,  $0 \leq V^i(X_k^i) \leq 1$
- ✓ Linear, concave, convex, S-shaped, etc.
- ✓ Presence of value functions allows for consideration of a broad range of indicators and relaxes need for using indicators with same units.

### Examples



Number of **new patents** used in building design



Annoyance to neighbours (**noise**) during construction

# PBE-Approach to the Holistic Best Design Decision

## □ MIVES: Decision-Making Process

### ▪ Weight Assignment

Requirement	$W_{req}$ %	Criteria	$W_{crit}$ %	$i$	Indicator	$W_{ind}$ %	Unit
Functional	10.0	Quality perception	30.0	1	User	75.0	0-5
				2	Visitor	25.0	0-5
		Adaptability to changes	70.0	3	Modularity	100.0	%
Economic	50.0	Construction cost	50.0	4	Direct cost	80.0	\$
				5	Deviation	20.0	%
		Life cost	50.0	6	Utilization	40.0	\$
				7	Maintenance	30.0	\$
<b>8</b>	<b>Losses</b>	<b>30.0</b>	<b>\$</b>				
Social	20.0	Integration of science	10.0	9	New patents	100.0	#
		⋮	⋮	⋮	⋮	⋮	⋮
Environmental	20.0	Construction	20.0	15	Water consumption	10.0	m <sup>3</sup>
				16	CO <sub>2</sub> emission	40.0	Kg
				17	Energy consumption	10.0	MJ
				18	Raw materials	20.0	Kg
				19	Solid waste	20.0	Kg
		Utilization	40.0	20	Noise, dust, smell	10.0	0-5
				21	Energy consumption	45.0	MJ/year
				22	CO <sub>2</sub> emission	45.0	kg/year
⋮	⋮	⋮	⋮	⋮	⋮		

Slides 9 to 11

# PBE-Approach to the Holistic Best Design Decision

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## □ MIVES: Decision-Making Process

### ▪ Selection Amongst Alternatives

Integration of values of every indicator of an alternative  $k$

$$V_k = \sum_{i=1}^{N_{ind}} W_{req}^i \cdot W_{crit}^i \cdot W_{ind}^i \cdot V^i(X_k^i)$$

Weights                      Value function

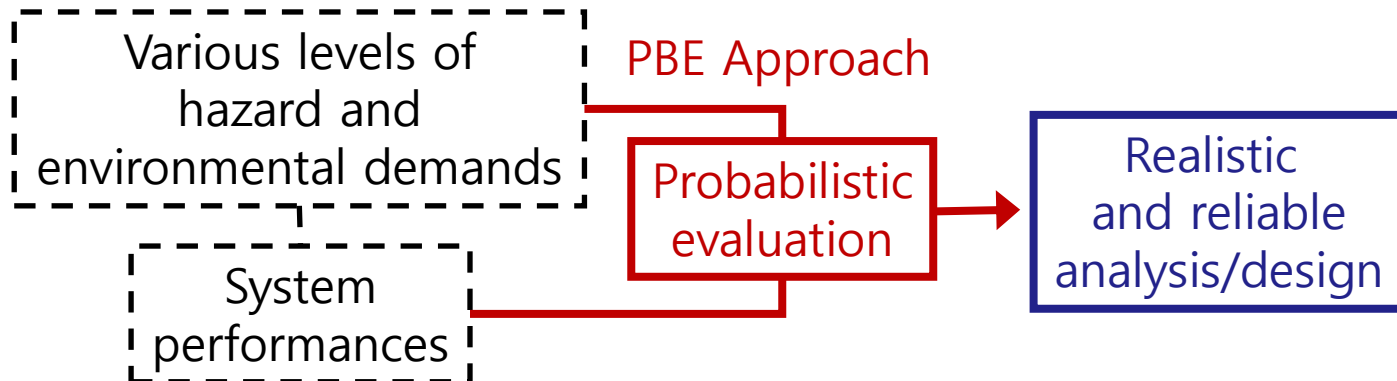
- ✓ The overall value of each alternative is determined →  
The alternative that has the **highest** value, i.e. closest to **1.0**, becomes the most suitable alternative, i.e. the **“best”** solution.

# PBE-Approach to the Holistic Best Design Decision

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## □ PBE approach

- Design framework resulting in the desired system performances at various intensity levels of hazards or environmental demands
- Explicit calculation of system performance measures in a rigorous probabilistic manner without heavily relying on expert opinion
- Outcome in terms of the direct interests of various stakeholders



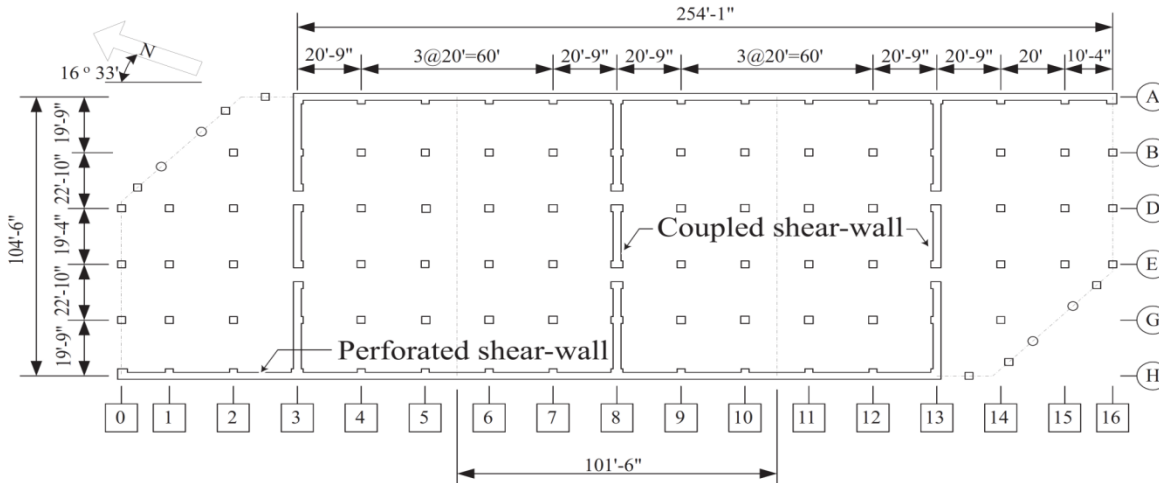
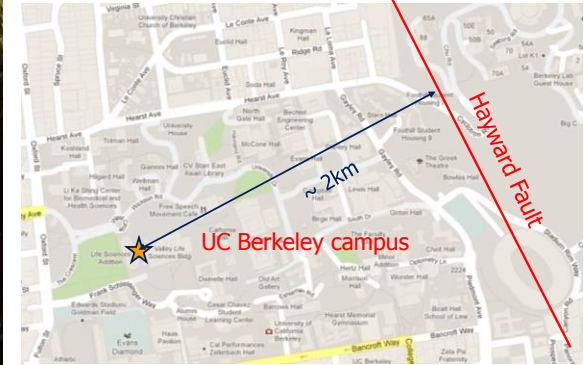


# Testbed for PBE-Approach

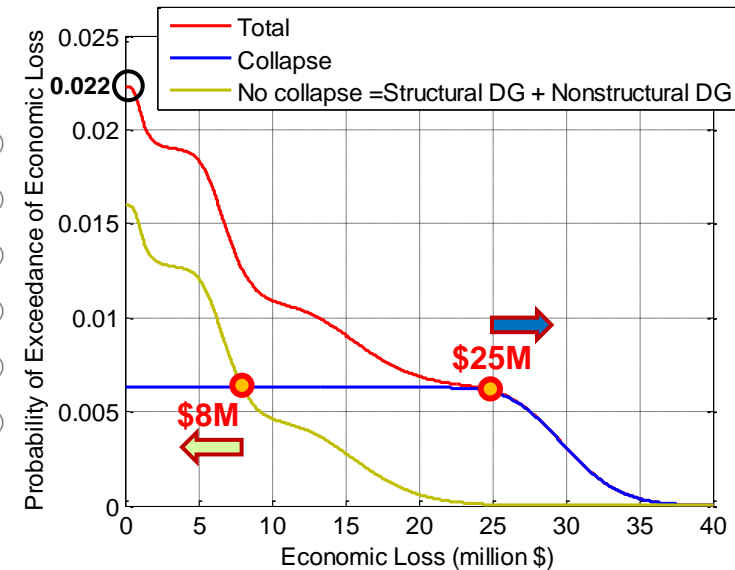
**Example building:** UCS building at UCB

Economic loss due to EQ [**2% POE in 50 years**]

POE and PDF can be calculated based on the total probability theorem.



Plan view of the UCS building located at UC-Berkeley campus  
Lee & Mosalam, 2006



**Loss Curve**  
Mosalam & Günay, 2011

# PBE-Approach: Extension to Indicators in the Tree

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## PBE for Earthquake Engineering

$$P(DV) = \sum [P(DV | EDP_{NC}, IM) \cdot p(EDP_{NC} | IM) + P(DV | EDP_C) \cdot p(EDP_C | IM)] \cdot p(IM)$$

- ✓ Intensity Measure (IM)
- ✓ Decision Variable (DV)
- ✓ Collapse (C) & No Collapse (NC)

For structural safety: IM can be  $S_a$  [spectral quantity] based on a certain POE & return period at a specific site.

## PBE for Sustainability

$$P(SDV) = \sum P(SDV | EM) \cdot p(EM | CV) \cdot p(CV)$$

- ✓ Climate Variable (CV)
- ✓ Energy Measure (EM)
- ✓ Sustainability Decision Variable (SDV)

For Indicators, e.g. sustainability decision variable such as CO<sub>2</sub> emission: IM can be substituted with one of the environmental demands, CV, e.g. average outdoor temperature.

# PBE-Approach: PBE-MIVES

## Multiple Indicators in a Direct Probabilistic Manner

Assume **3** indicators  $DV_{CO_2}$ ,  $DV_E$  and  $DV_{ST}$  with PDFs:

$$f_{CO_2}(DV_{CO_2} = a) = A, \quad f_E(DV_E = b) = B, \quad f_{ST}(DV_{ST} = c) = C$$

**Weights:**  $w_{CO_2}$ ,  $w_E$  &  $w_{ST}$ , **Value functions:**  $u_{CO_2}$ ,  $u_E$ , &  $u_{ST} \rightarrow$  Overall value for the indicators:

$$V(a, b, c) = V_{CO_2}(a) + V_E(b) + V_{ST}(c) = w_{CO_2}u_{CO_2}(a) + w_Eu_E(b) + w_{ST}u_{ST}(c)$$

If  $DV_{CO_2}$ ,  $DV_E$  &  $DV_{ST}$  are **mutually independent**, the joint PDF is:

$$\begin{aligned} f(a, b, c) &= f_{CO_2, E, ST}(DV_{CO_2} = a, DV_E = b, DV_{ST} = c) \\ &= f_{CO_2}(DV_{CO_2} = a) f_E(DV_E = b) f_{ST}(DV_{ST} = c) = ABC \end{aligned}$$

**else,**

$$\begin{aligned} f(a, b, c) &= f_{CO_2, E, ST}(DV_{CO_2} = a, DV_E = b, DV_{ST} = c) \\ &= f_{CO_2}(DV_{CO_2} = a) f_{E|CO_2}(DV_E = b | DV_{CO_2} = a) f_{ST|CO_2, E}(DV_{ST} = c | DV_{CO_2} = a, DV_E = b) \end{aligned}$$

**Conditional probability distribution** should be defined.

$$P(DV^n = a) = p(DV > DV^n = a) = \int_a^\infty f_{DV}(DV) d(DV)$$

$P(DV^n)$ : POE of  $n^{\text{th}}$  value of  $DV$ ,  $p(DV > DV^n = a)$ : probability of  $DV$  exceeding  $a$ , the  $n^{\text{th}}$  value of  $DV$ .

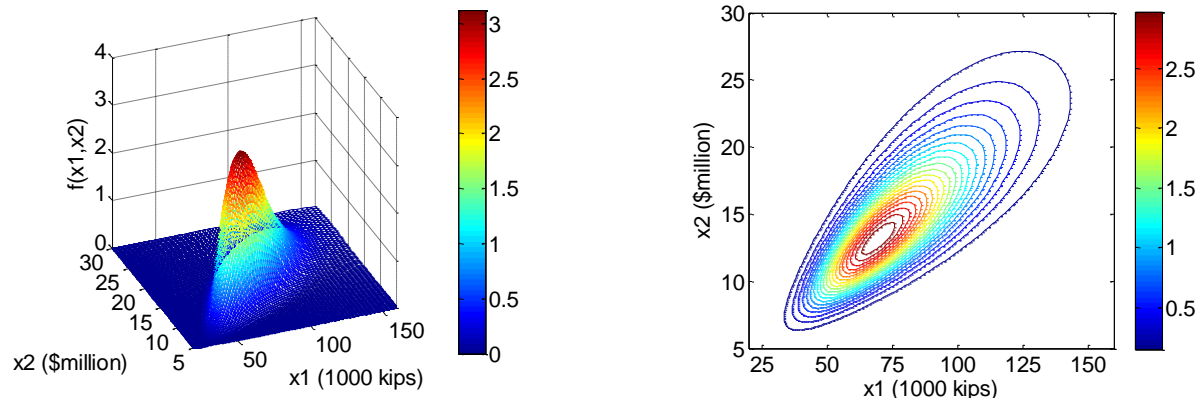
# PBE-MIVES: Application to the UCS Building

- **Two alternatives with different fuel consumption ratios**

Electricity : Natural gas = 5 : 2 (**Plan 1**) in Btu, Electricity only (**Plan 2**)

- **Assumptions for the energy expenditure and CO<sub>2</sub> emission**

- ✓ Bivariate lognormal distribution assumed for energy expenditure and CO<sub>2</sub> emission for **50 years (building life span)**.
- ✓ Each mean value estimated based on data for **office buildings** in the West-Pacific region (by DOE, EIA, & EPA).
- ✓ Standard deviation assumed as **30%** of the corresponding mean value.
- ✓ Coefficient of correlation assumed as **0.8**.



Probability density function of CO<sub>2</sub> emission ( $x_1$ ) and energy expenditure ( $x_2$ ) for **Plan 1**

# PBE-MIVES: Application to the UCS Building

## Tree Construction and Weight Assignment

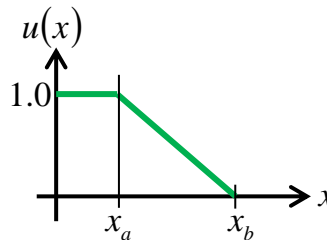
Requirement	$W_r$ [%]	Criteria	$i$	Indicator	$W_i$ [%]	Unit
Environmental	25.0	Utilization	1	CO <sub>2</sub> emissions	100.0	1000 kips
Economic	75.0	Life cost	2	Energy expenditures	60.0	\$million
			3	Losses	40.0	\$million

correlated

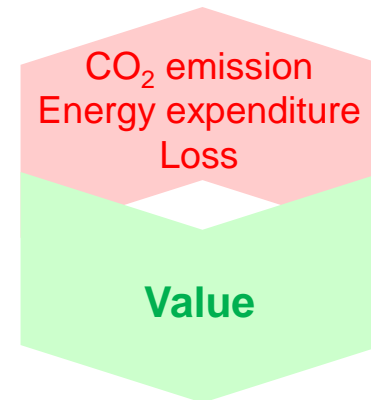
independent

## Value Functions

Linearly decreasing value function is used for each indicator.



$$\begin{aligned}
 u(x) &= 1.0 \quad \text{if } x \leq x_a \\
 &= 1.0 - (x - x_a) / (x_b - x_a) \quad \text{if } x_a < x \leq x_b \\
 &= 0.0 \quad \text{if } x > x_b
 \end{aligned}$$



# PBE-MIVES: Application to the UCS Building

## Selection Amongst Alternatives

$$V_{prob} = \int_{\Omega} Vf d\Omega$$

The expected value of each alternative in a pre-defined domain  $\rightarrow$  rank alternatives

No economic loss due to EQ, i.e.  $x_3 = 0$

Case 1:  $0 \leq x_1 \leq 80, 0 \leq x_2 \leq 15$

Plan 1:  $V_{prob} = 309.52$   $\leftarrow$

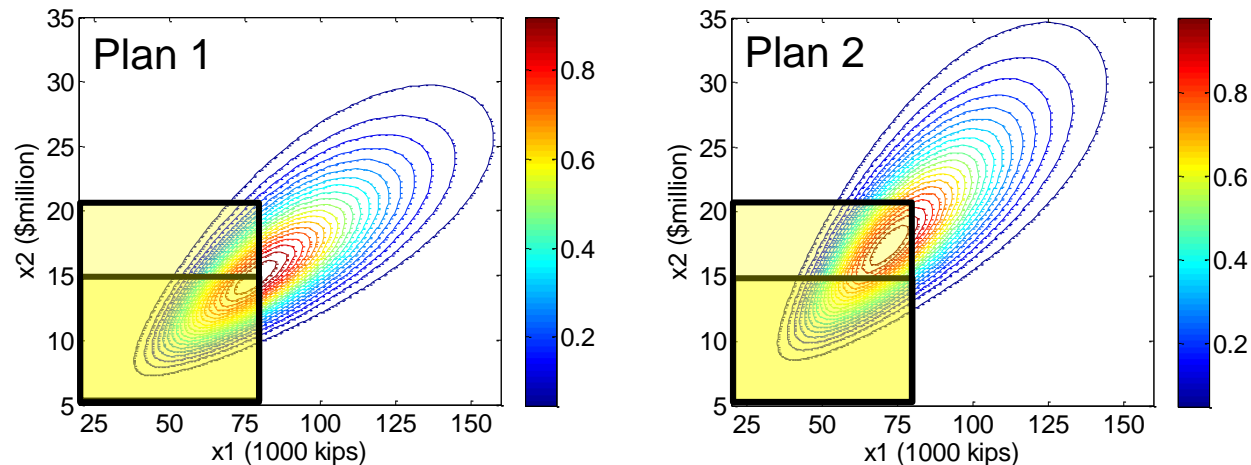
Plan 2:  $V_{prob} = 223.56$

Case 2:  $0 \leq x_1 \leq 80, 0 \leq x_2 \leq 20$

Plan 1:  $V_{prob} = 393.95$

Plan 2:  $V_{prob} = 449.61$   $\leftarrow$

*Domain Dependency !*



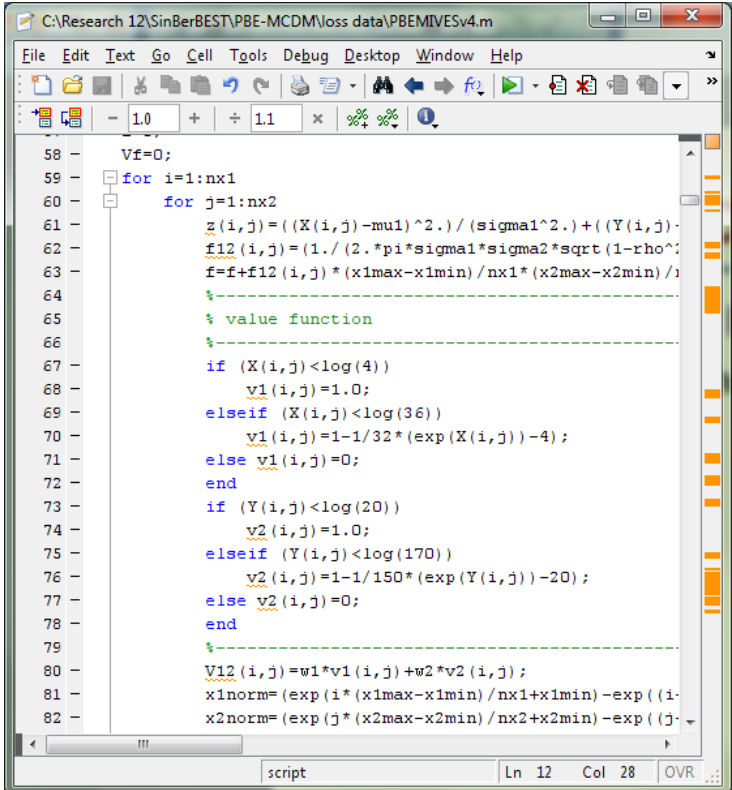
Contours of  $Vf$  of CO<sub>2</sub> emissions ( $x_1$ ) and energy expenditures ( $x_2$ ) for Plans 1 and 2 of the UCS example building

[Monetary loss due to structural damages  $x_3 = 0$ ]

# Concluding Remarks

- ✓ The probabilistic nature of the indicators can be considered in MCDA either indirectly by calculating the value of each indicator in a probabilistic manner or directly by formulating the value determination equation in a probabilistic framework.
- ✓ The correlation between the different indicators is taken into account in the direct formulation and it is the preferred method when there is significant interdependency between indicators.
- ✓ In the comparison of  $V_{prob}$  in the UCS application building, considered range of indicators can change the value of the alternatives and affect the final decision. Attention should be paid to the selection of the proper range of indicators.

## Matlab code for PBE-MIVES



```
58 - Vf=0;
59 - for i=1:nx1
60 -     for j=1:nx2
61 -         z(i,j)=((X(i,j)-mu1)^2.)/(sigma1^2.)+(Y(i,j)-mu2)^2.)/(sigma2^2.);
62 -         f12(i,j)=(1./(2.*pi*sigma1*sigma2*sqrt(1-rho^2.)))*exp(-z(i,j)/2.);
63 -         f=f+f12(i,j)*(x1max-x1min)/nx1*(x2max-x2min)/nx2;
64 -     end
65 -     % value function
66 -     %-----
67 -     if (X(i,j)<log(4))
68 -         v1(i,j)=1.0;
69 -     elseif (X(i,j)<log(36))
70 -         v1(i,j)=1-1/32*(exp(X(i,j))-4);
71 -     else v1(i,j)=0;
72 -     end
73 -     if (Y(i,j)<log(20))
74 -         v2(i,j)=1.0;
75 -     elseif (Y(i,j)<log(170))
76 -         v2(i,j)=1-1/150*(exp(Y(i,j))-20);
77 -     else v2(i,j)=0;
78 -     end
79 -     %-----
80 -     V12(i,j)=w1*v1(i,j)+w2*v2(i,j);
81 -     x1norm=(exp(i*(x1max-x1min)/nx1+x1min)-exp(i*(x1min-x1max)/nx1))/((x1max-x1min)/nx1);
82 -     x2norm=(exp(j*(x2max-x2min)/nx2+x2min)-exp(j*(x2min-x2max)/nx2))/((x2max-x2min)/nx2);
```

# Future Work

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- ✓ Selecting major indicators (**including those for safety and health in construction activities**) and corresponding weights in office building design
- ✓ Collecting data/defining probability distributions & correlations for office buildings in the tropics
- ✓ Accounting for results obtained from various testbeds, e.g. on newly developed façade systems
- ✓ Evaluating the efficiency of a newly developed technologies, e.g. novel façade systems



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***Thank You!***  
***Questions? Comments?***